

HW 2.1

Wrectangle	80	mm	
Hrectangle	100	mm	
Wsquare	40	mm	
Hsquare	40	mm	Square could be rectangular!
PosnSquare	60	mm	

Arectangle	8000	mm ²	=Wrectangle*Hrectangle
Asquare	-1600	mm ²	=-Wsquare*Hsquare
Atotal	6400	mm ²	=Arectangle+Asquare

Calculate the location of the Neutral Axis of the combined shape.

Rtot	47.500	mm	=(Arectangle*Hrectangle/2+Asquare*PosnSquare)/Atotal
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Area Moments of Inertia of the Rectangle and Square about their own centroids.

The Square is negative because it is a hole.

Irectangle	6,666,666.67	mm ⁴	=Wrectangle*Hrectangle ³ /12
Isquare	-213,333	mm ⁴	=-Wsquare*Hsquare ³ /12

These are the distances that the centroids of the Rectangle and the Square are from the centroid of the combined shape.

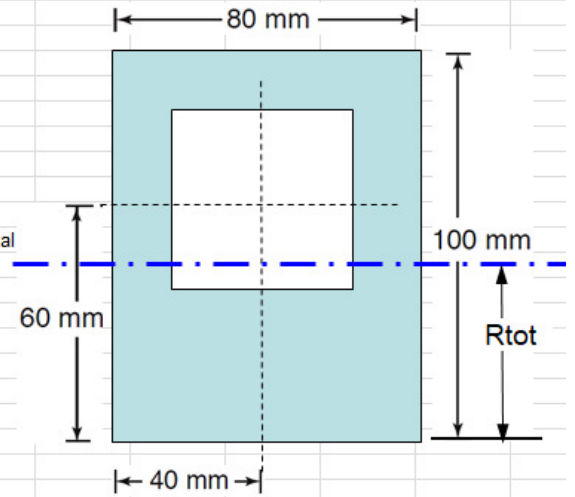
d_Rect	2.5	mm	=Hrectangle/2-Rtot
d_Square	12.5	mm	=PosnSquare-Rtot

This is the Area of the Rectangle and Square times the square of the distances from their centroids to the new centroid

Ad2_rect	50,000	mm ⁴	=Arectangle*d_Rect ²
Ad2_sqr	-250,000	mm ⁴	=Asquare*d_Square ²

Now the result of the Parallel Axis Theorem

Ishift_rect	6,716,666.67	mm ⁴	=Irectangle+Ad2_rect
Ishift_sqr	-463,333.33	mm ⁴	=Isquare+Ad2_sqr
I total	6,253,333	mm ⁴	=Ishift_rect+Ishift_sqr



HW 2.2

L	500	m
P	5	MN
Sigma	150	N/mm ²
E	70000	Mpa

Because Stress, Sigma = P/A

A	0.0333	m ²	=P/Sigma
Amm	33333.33	mm ²	=A*1,000,000

Radius	103.01	mm	=SQRT(Amm/PI())
Dia	206.01	mm	=2*Radius

Strain	0.002143		=Sigma/E	$\sigma = \epsilon E$
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Delta	1.071	m	=Strain*L	$\epsilon = \frac{\Delta L}{L}$
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also	1.071	m	=P*L/(A*E)	$y = \frac{PL}{AE}$
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Stiffness = Load / Deflection

K	4.667	MN/m	=P/Delta
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HW 2.3

Power	500,000	W
RPM	3600	
TauMax	60,000,000	N/m ²

Convert RPM to Radians/sec

$$\text{Rad/sec} = 376.991 \text{ s}^{-1} = \text{RPM}/60 * 2 * \text{PI}()$$

$$\text{Torque} = 1326.291 \text{ Nm} = \text{Power}/\text{Rad_sec}$$

Torsional Shear = T/r

For a circular cross section, $J = \text{Pi}/2 * r^4$

$$\text{or } J = \text{Pi}/32 * d^4$$

$$\tau = \frac{Tr}{J}$$

$$J = \frac{\pi}{2} r^4 = \frac{\pi}{32} d^4$$

Then Torsional Shear = $T * (d/2) / (\text{Pi}/32 * d^4)$

$$\text{or } = T / (\text{Pi}/16 * d^3)$$

$$D^3 = 0.0001126 \text{ m}^3 = 16 * \text{Torque} / (\text{Pi}() * \text{TauMax})$$

$$D = 0.04828578 \text{ m} = D_3^{(1/3)}$$

$$48.29 \text{ mm} = D * 1000$$

HW 2.4

Ro	300	mm	
Ri	240	mm	
W	120	mm	Width
M	4000	Nm	Moment

This is a rectangular shape, so the Neutral Radius is

$$R_n = 268.885 \text{ mm} = (R_o - R_i) / (\text{LN}(R_o/R_i))$$

The Centroidal Radius is

$$R_c = 270 \text{ mm} = (R_o + R_i) / 2$$

Eccentricity

$$e = 1.1148 \text{ mm} = R_c - R_n$$

Cross Sectional Area

$$A = 7200 \text{ mm}^2 = (R_o - R_i) * W$$

Distances from Neutral Axis to Inner and Outer surfaces

$$C_i = 28.885 \text{ mm} = (R_o - R_i) / 2 - e$$

$$C_o = 31.115 \text{ mm} = (R_o - R_i) / 2 + e$$

Stresses at Inner and Outer Surfaces

Inner is Tensile because arc is being stretched open.

Outer is Compressive.

$$\text{Sigma}_i = 59.979 \text{ MPa} = M * C_i / (A * e * R_i) * 1000$$

$$\text{Sigma}_o = 51.687 \text{ MPa} = M * C_o / (A * e * R_o) * 1000$$

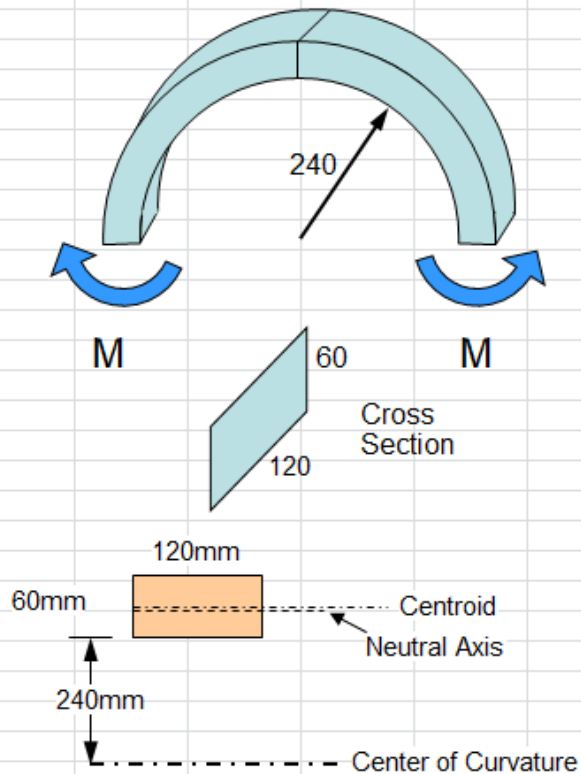
Area Moment of Inertia

$$I = 2,160,000 \text{ mm}^4 = W * (R_o - R_i)^3 / 12$$

The bending stress if the bar wasn't curved = Mc/I

$$\text{Sigma} = 55.56 \text{ MPa} = M * 0.5 * (R_o - R_i) / I * 1000$$

This value is between Sigma_i and Sigma_o - where it should be.



HW 2.5

OD	100	mm	Outer Diameter
T	10	mm	Wall Thickness
L	1.2	m	Length
F	15000	N	Force

Ro	50.00	mm	=OD/2
Ri	40.00	mm	=Ro-T

MomOfI	2,898,119.22	mm ⁴	=PI()/4*(Ro ⁴ -Ri ⁴)
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M	18,000.00	Nm	=F*L
c	50	mm	=Ro

Convert Nm to Nmm by multiplying by 1000. Newtons/mm² = MPa

SigmaBend	310.546	MPa	=M*c_/MomOfI*1000
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Calculate transverse shear: 2F/A for a hollow tube.

Area	2827.433	mm ²	=PI()* (Ro ² -Ri ²)
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Shear	10.610	MPa	=2*F/Area
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